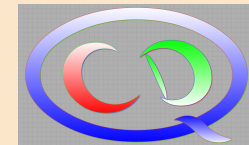


# Symmetries and the Emergence of Structure in QCD

– Introduction to the CRC 110 –



Ulf-G. Meißner, Univ. Bonn & FZ Jülich

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- The CRC 110
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# The CRC 110

# What is a Collaborative Research Center?

Collaborative Research Centres (CRCs) are institutions established at universities for a period of up to 12 years that enable researchers to pursue an **outstanding research programme**, crossing the boundaries of disciplines, institutes, departments and faculties. They facilitate **scientifically ambitious, complex, long-term research** by concentrating and coordinating the resources available at a/up to three university/ties. Universities submitting a proposal are expected to provide appropriate core support. The CRC programme should, thus, contribute towards defining the profiles of participating universities. Gender equality and early career support are additional goals of a Collaborative Research Centre.

Collaborative Research Centres may also incorporate projects at neighbouring universities or non-university research institutions and collaboration with industry and business within the research programme, provided they serve to further the core research area. In addition, **CRCs maintain scientific relations with universities and other research institutions outside of Germany**. *Co-funding for international CRCs is also possible.*

[http://www.dfg.de/en/research\\_funding/programmes/coordinated\\_programmes/collaborative\\_research\\_centres/index.html](http://www.dfg.de/en/research_funding/programmes/coordinated_programmes/collaborative_research_centres/index.html)

# The partners



***Institute of High Energy Physics, CAS, Beijing***

***Peking University***

***Theoretical Center for Science Facilities, CAS***



***Rheinische-Friedrich-Wilhelms-Universität Bonn***

***Forschungszentrum Jülich***

***Technische Universität München***

- Comprehensive university (Volluniversität)
- 7 faculties, about 30.000 students
- research foci: Mathematics (Cluster of Excellence)  
Physics and Astronomy (Bonn-Cologne Graduate School)  
Life sciences  
Economy
- 3 main research areas in physics:  
**Particle & hadron physics**, astrophysics, photonics and condensed matter
- physics high-lights:  
Nobel prize physics 1989 Wolfgang Paul  
Electron Stretcher Accelerator ELSA & CRC 16 “Subnuclear Structure of Matter”  
Bethe Center for Theoretical Physics & Bethe Forum (new)



# Forschungszentrum Jülich

- Large interdisciplinary research center
- 11 institutes, about 4500 employees
- research foci: Information technologies  
Energy and environment  
Health
- main research areas in physics:  
**Hadron & nuclear physics**, condensed matter physics, computational physics
- physics high-lights:  
Nobel prize physics 2007 Peter Grünberg  
Cooler Synchrotron COSY  
& construction of the HESR at FAIR  
Jülich Supercomputing Center





- Technical university  
(*Exzellenz-Universität*)
- 13 faculties, about 26.000 students
- research foci: Mathematics & Informatics  
Physics  
Chemistry & Life Sciences  
Engineering
- 3 main research areas in physics:  
**Nuclear, particle & astrophysics**, condensed matter physics, biophysics
- Munich physics high-lights:  
Nobel prize physics 1961 R. Mößbauer (TUM), 1985 Klaus von Klitzing (TUM)  
Cluster of excellence “Origin and Structure of the Universe”  
Institute for Advanced Studies (TUM-IAS) and Leibniz Supercomputing Center





# Institute of High-Energy Physics (IHEP)

- **Top institution in China for high-energy and hadron physics**
- hosts 3 big international experimental facilities
  - BEPC2 w/ BESIII collaboration
  - Daya Bay neutrino experiment
  - Tibet cosmic ray observatory
- 7 research divisions with about 750 researchers
  - Accelerator Center, Experimental Physics Center, Theory Division, Particle-Astroparticle Center, Computing Center, Technology R&D Center, Multi-disciplinary Center
- Host of the **Theoretical Center for Science Facilities**
  - improve the theory support of the chinese facilities





# Why this collaboration?

- Very challenging endeavour, requires complementary and overlapping expertise  
⇒ this is available at the various institutions forming this CRC
- Large investment in facilities requires concentrated theory effort  
⇒ strong focus on data from BEPC-II (now) and FAIR (future)
- Improving the bilateral scientific relations  
⇒ best use of the science brain pool in both countries
- Builds on earlier and on-going collaborations by some of the PIs  
⇒ [Brambilla, Vairo, Jia], [Guo, Hanhart, Meißner, Zhao], [Hanhart, Guo, Zou]  
[Kaiser, Meißner, Weise], [Rusetsky, Weise], [Dreiner, Hanhart], ...

⇒ Potential for a long-term synergy and innovation  
very much desired by the partners

# Principal Investigators (PIs)

- Principal investigators:

**IHEP** Prof. Y. Chen, Prof. Y. Dong,  
Prof. M. Huang, Prof. Y. Jia,  
Prof. J.-X. Wang, Prof. P. Wang,  
Prof. Q. Zhao, Prof. B.-S. Zou



**PKU** Prof. C. Liu, Prof. S.-L. Zhu



**UB** Prof. H. Dreiner, Dr. F.-K. Guo, Prof. H.-W. Hammer,  
PD B. Kubis, Prof. U.-G. Meißner,  
PD A. Rusetsky, Prof. C. Urbach



**FZJ** PD J. Haidenbauer, PD C. Hanhart, [Prof. U.-G. Meißner],  
Dr. A. Nogga, *Prof. N.N.*[comp. nuclear physics]



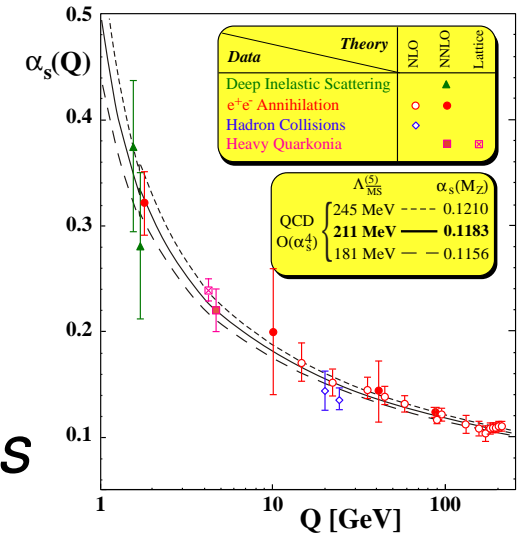
**TUM** Prof. N. Brambilla, Prof. N. Kaiser,  
PD A. Vairo, Prof. W. Weise



# Topics in Strong QCD

# Facets of Quantum Chromodynamics

- perturbative QCD: quarks, gluons, . . .
  - **strong** QCD: hadrons, nuclei, . . .
  - a plethora of *structures* and (*broken*) *symmetries*
  - Aspects of QCD in the **CRC 110**:
    - decays and interactions of hadrons (esp. charm sector)
    - how QCD generates structures: hadrons, nuclei, . . .
    - precision calculations to test physics beyond the SM
- *interplay of lattice QCD, EFTs and models*



## Role of CRC 110

- Two loose ends of the Standard Model:
  - the Higgs boson (EW symmetry breaking)
  - structure and dynamics of **strong QCD**

**Unique contribution of CRC 110 to **strong QCD**:**

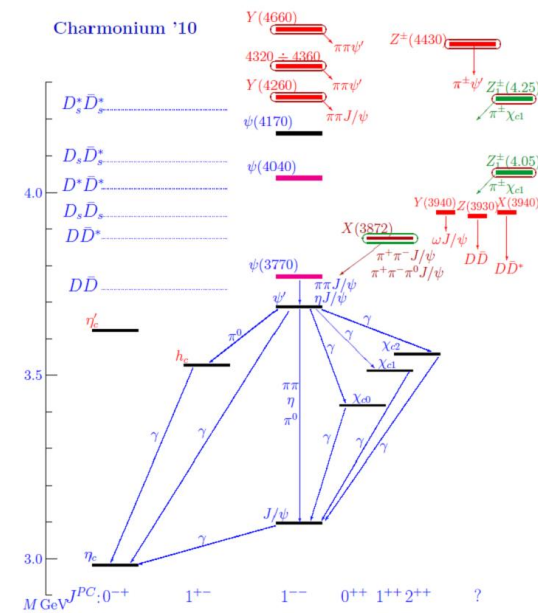
**Investigation of how QCD generates structures:  
hadrons, nuclei, . . . and how symmetries  
influence their structure and dynamics  
based on a large international collaboration**

- For the first time, such a unified approach is attempted

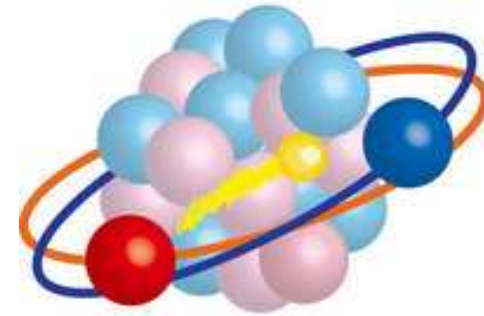


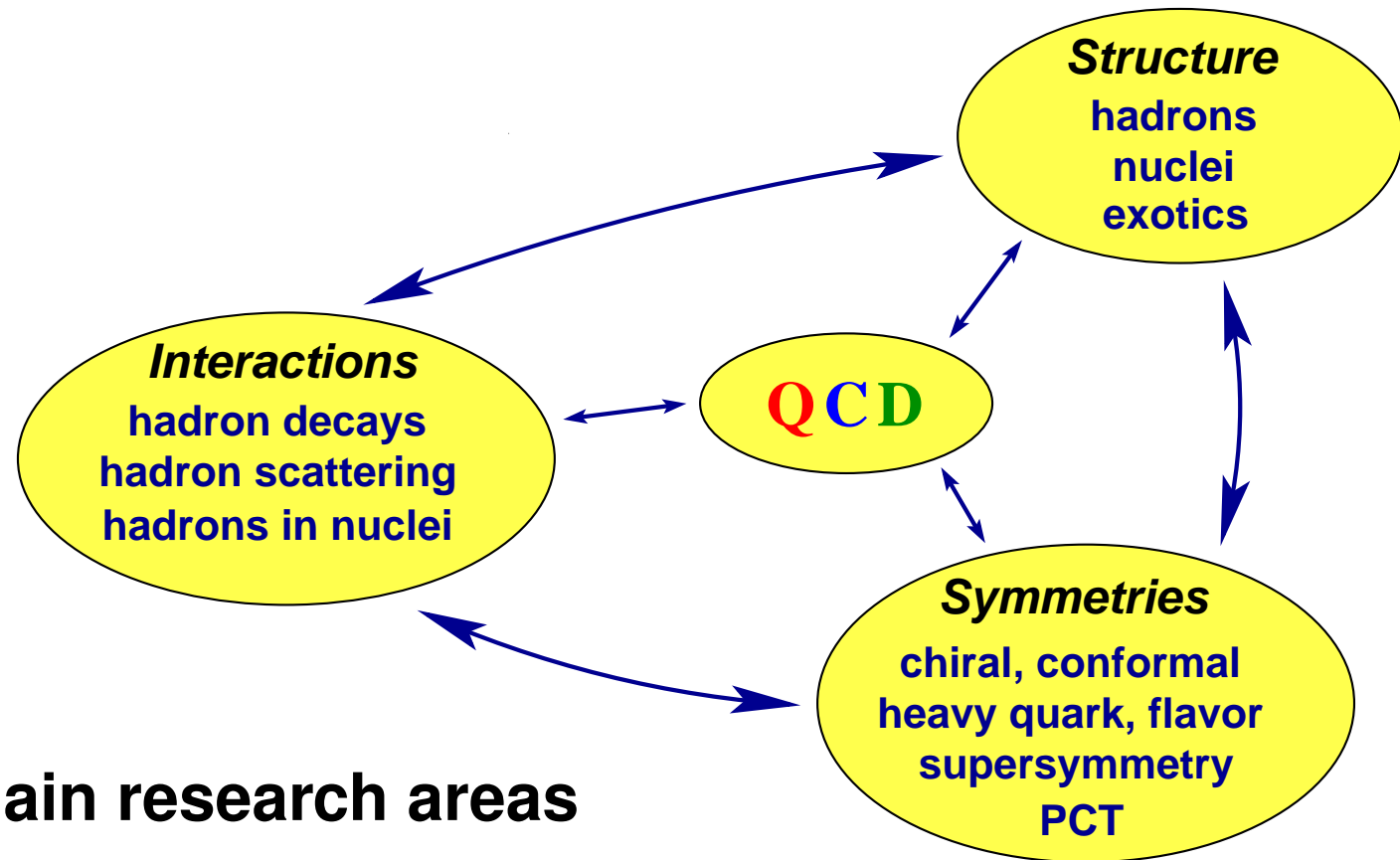
# FACETS of STRONG QCD

- quarks and gluons form hadrons
  - ⇒ **lattice QCD + EFT + models**
  - ⇒ **exploring the strong color force**



- nucleons and mesons form nuclei
  - ⇒ **nuclear physics (EFT, lattice, ...)**
  - ⇒ **exploring the residual color force**





- **CRC 110: two main research areas**

*A – symmetries*

*B – emergence of structure*

- **strongly intertwined**

- Project area A: **Symmetries**

- |     |  |                         |
|-----|--|-------------------------|
| A.1 | Flavor symmetries and FSI in heavy hadron decays | Haidenbauer, Kubis, Zou |
| A.2 | Hadron-hadron scattering in QCD                  | Liu, Urbach             |
| A.3 | Universality and EFT for threshold states        | Brambilla, Hammer, Jia  |
| A.4 | Hadronic parity violation                        | Kaiser, Zhu             |
| A.5 | Quark mass dependence of heavy-light systems     | Guo, Meißner, P. Wang   |

- Project area B: **Emergence of Structure**

- |     |   |                        |
|-----|---|------------------------|
| B.1 | Nucleon form factors  | Dong, Hammer           |
| B.2 | Hadron spectroscopy   | Huang, Zhu, Zou        |
| B.3 | Hadronic molecules with heavy meson loops                       | Hanhart, Guo, Zhao     |
| B.4 | Boxed exotica   | Liu, Rusetsky          |
| B.5 | Exotic states from lattice QCD                                  | Chen, Urbach           |
| B.6 | Hadronic systems with strange quarks                            | Rusetsky, Weise        |
| B.7 | Chiral dynamics of nuclei & hypernuclei                         | Meißner, Nogga, Kaiser |
| B.8 | Quarkonium interactions in hadronic, nuclear and thermal matter | Jia, Vairo, J. Wang    |

⇒ 10 of 13 projects have chinese & german project leaders!

# Scientific goals

- Symmetry tests in hadrons and nuclei & precision calculations

A.1,A.2,A.3,A.4,B.3,B.6

- Structure and dynamics of (heavy) hadrons

A.1,A.2,A.3,A.5,B.1,B.2,B.3,B.4,B.5,B.6

- QCD-based structure of nuclei, hypernuclei and nuclear matter

A.2,A.4,B.6,B.7,B.8

- *note: many further cross-links by use of common (non-perturbative) methods*

# Ex. 1: Isospin violation & light quark masses

- Isospin violation has two sources (QCD + QED):

$$\mathcal{H}_{\text{QCD}}(x) = \frac{1}{2}(m_d - m_u)(\bar{d}d - \bar{u}u)(x)$$

$$\mathcal{H}_{\text{QED}}(x) = -\frac{1}{2}e^2 \int dy D^{\mu\nu}(x - y)T(j_\mu(x)j_\nu(y))$$

⇒ *unique window to quark masses for light quark and heavy-light quark systems*

- Both effects usually small *and* of the same size (e.g.  $m_p - m_n$ )

⇒ systematic machinery must cope with both these accurately

- Chiral perturbation theory w/ virtual photons is the tool to analyse the strictures of the spontaneously and explicitly broken chiral symmetry of **QCD**
- Lattice QCD: strong splittings, EM still not solved (first steps)

# GENERAL REMARKS

- Can be probed in a plethora of Goldstone-boson N-point functions

⇒ requires high-precision calcs (e.g. GB masses)

Gasser, Leutwyler, ...

- Isospin violation is enhanced in system with nucleons and (neutral) pions

Weinberg 1977

$$a(\pi^0 p) - a(\pi^0 n) = \frac{m_p c_5 B(m_d - m_u)}{\pi(m_p + M_\pi) F_\pi^2} = (-2.3 \pm 0.4) \cdot 10^{-3} / M_\pi$$

→ precision data from hadronic atoms and threshold pion photoproduction

- further suppression in some processes involving two or more nucleons (CSB)

→ pioneering data on  $A_{fb}(np \rightarrow d\pi^0)$  [TRIUMF] and  $\sigma(dd \rightarrow \alpha\pi^0)$  [IUCF]

- systems with **heavy** quarks can give additional information on  $m_u - m_d$  through decays and mass differences



# THE PUZZLE of $m_u/m_d$ EXTRACTIONS

- Extract  $m_u/m_d$  from  $\psi' \rightarrow J/\psi\pi^0(\eta)$

Ioffe, Shifman, 1980; Donoghue et al., 1982

$$R_{\pi^0/\eta} = \frac{\mathcal{B}(\psi' \rightarrow J/\psi\pi^0)}{\mathcal{B}(\psi' \rightarrow J/\psi\eta)} = 3 \left( \frac{m_d - m_u}{m_d + m_u} \right)^2 \frac{F_\pi^2 M_\pi^4}{F_\eta^2 M_\eta^4} \left| \frac{\vec{q}_\pi}{\vec{q}_\eta} \right|^3 (1 + \Delta)$$

⇒ using CLEO data (2008):  $\frac{m_u}{m_d} = 0.40 \pm 0.01$

- Extraction from the Goldstone bosons mass ratios:

Weinberg, 1977; Gasser and Leutwyler, 1982; Leutwyler, 1996

$$\frac{m_u}{m_d} = \frac{M_{K^+}^2 - M_{K^0}^2 + 2M_{\pi^0}^2 - M_{\pi^+}^2}{M_{K^0}^2 - M_{K^+}^2 + M_{\pi^+}^2} (1 + \Delta^{\text{str}} + \Delta^{\text{em}}) = 0.553 \pm 0.043$$

⇒

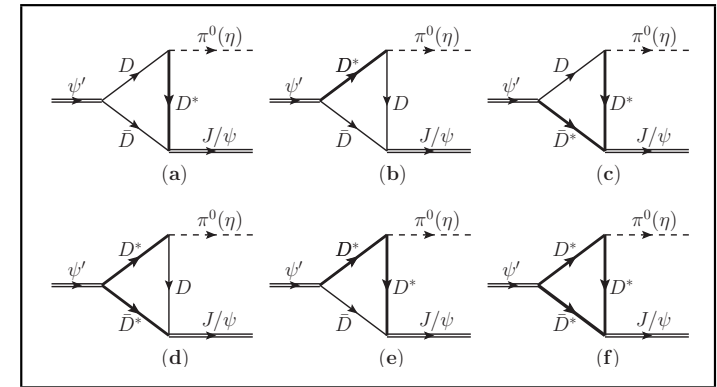
serious discrepancy

# INCLUSION of CHARMED MESON LOOPS

Guo, Hanhart, UGM, Phys. Rev. Lett. **103** (2009) 082003

- consider intermediate charmed mesons
- HQEFT (velocity) expansion:

$$v \sim \sqrt{(2M_{\hat{D}} - M_{\hat{\psi}})/M_{\hat{D}}} \simeq 0.5$$



- direct versus charmed meson loop contribution:

$$\mathcal{M}(\psi' \rightarrow J/\psi \pi^0)_{\text{direct}} \sim (m_d - m_u) |\vec{q}_\pi|$$

$$\mathcal{M}(\psi' \rightarrow J/\psi \pi^0)_{\text{D-loops}} \sim (m_d - m_u) \frac{|\vec{q}_\pi|}{v} \Leftarrow \text{enhancement}$$

- charmed meson loop saturation:  $R_{\pi^0/\eta} = 0.11 \pm 0.06$

$$R_{\pi^0/\eta}^{\text{exp}} = 0.0388 \pm 0.023 \pm 0.005$$



need an NLO calculation to see how accurately  $m_u/m_d$  can be extracted from these decays

# BETTER NEWS: BOTTONOMIUM TRANSITIONS

Guo, Hanhart, UGM, Phys. Rev. Lett. **105** (2010) 162001

- Consider bottomonium transitions:  $\Upsilon(4S) \rightarrow h_b \pi^0(\eta)$

- Loops are suppressed for two reasons:

$$\star \vec{q}^2 / (v^3 M_B^2) \simeq 0.6 \text{ (0.2)}$$

$$\star M_{B^0} - M_{B^+} = 0.33 \pm 0.06 \text{ MeV} \ll m_d - m_u$$

due to strong & em interference

Guo, Hanhart, UGM, JHEP **0809** (2008) 136

$$\Rightarrow r = \frac{m_d - m_u}{m_d + m_u} \frac{m_s + \hat{m}}{m_s - \hat{m}} \text{ can be extracted with an accuracy of about 23 \%}$$

- by-product:  $\Upsilon(4S) \rightarrow h_b \eta$  is a nice channel to search for the  $h_b$   
(sizeable bf  $\sim 10^{-3}$ )

$\Rightarrow$  possible to measure at LHCb

# FORWARD-BACKWARD ASYMMETRY in $np \rightarrow d\pi^0$

- CSB fb-asymmetry in  $np \rightarrow d\pi^0$  @ 279.5 MeV measured at TRIUMF

Opper et al., 2003

$$A_{fb} = \frac{\int_0^{\pi/2} \left[ \frac{d\sigma}{d\Omega}(\theta) - \frac{d\sigma}{d\Omega}(\pi - \theta) \right] d\cos\theta}{\int_0^{\pi/2} \left[ \frac{d\sigma}{d\Omega}(\theta) + \frac{d\sigma}{d\Omega}(\pi - \theta) \right] d\cos\theta} = (17.2 \pm 8(\text{stat}) \pm 5.5(\text{sys})) \cdot 10^{-4}$$

- Goal: use the measured fb-asymmetry to extract the (strong) proton-neutron mass difference  $\delta m_N \equiv m_n - m_p$

- best determination: use the Cottingham sum rule

Gasser, Leutwyler, 1982

$$\delta m_N^{\text{str}} = 2.05 \pm 0.30 \text{ MeV}$$

$$\delta m_N^{\text{em}} = -0.76 \mp 0.30 \text{ MeV}$$

- pioneering calculations for  $A_{fb}$ :

Niskanen 1999, van Kolck et al., 2000

# THEORY of $A_{fb}$ in $np \rightarrow d\pi^0$

- CSB fb-asymmetry through interference of IC and IV amplitudes:

$$\frac{d\sigma}{d\Omega} = A_0 + A_1 P_1(\cos \theta_\pi) + A_2 P_2(\cos \theta_\pi) + \dots \implies A_{fb} \simeq \frac{A_1}{2A_0}$$

- $A_0$  can be determined from pionic deuterium lifetime measured at PSI:

$$\sigma(np \rightarrow d\pi^0) = \frac{1}{2}\sigma(nn \rightarrow d\pi^-) = 252_{-11}^{+5} \eta [\mu\text{b}] \rightarrow A_0 = 10.0_{-0.4}^{+0.2} \eta [\mu\text{b}]$$

Hauser et al., 1998

- $A_1$  at LO in chiral EFT:

$$A_1 = \frac{1}{128\pi^2} \frac{\eta M_\pi}{p(M_\pi + m_d)^2} \text{Re} \left[ \underbrace{\left( M_1 S_0 \rightarrow {}^3S_{1,p} + \frac{2}{3} M_1 D_2 \rightarrow {}^3S_{1,p} \right)}_{\text{IC amplitude calculated at NLO}} M_1^* P_1 \rightarrow {}^3S_{1,p} \right]$$

IC amplitude calculated at NLO

Hanhart et al., 2000

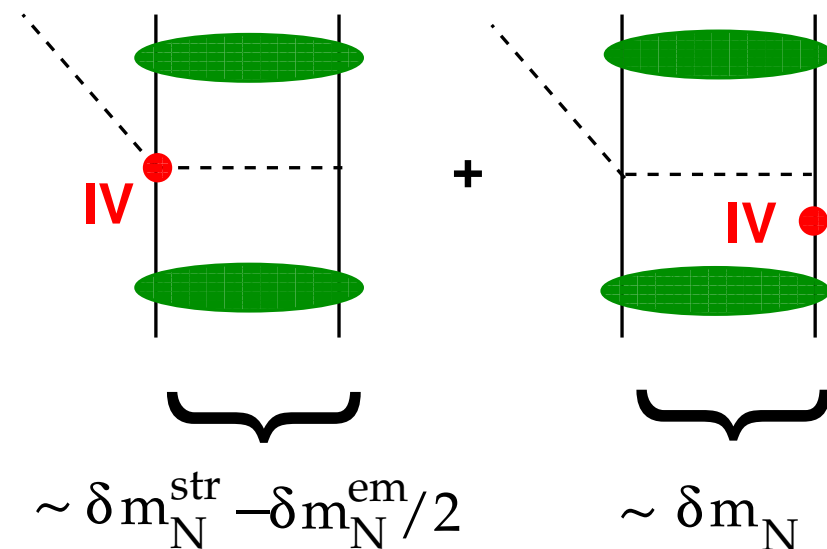
Baru et al., 2009

# EXTRACTION of $\delta m_N$ from $A_{fb}(np \rightarrow d\pi^0)$

- Both diagrams combine so that only  $\delta m_N^{\text{str}}$  survives

- so that we obtain

$$A_{fb}^{\text{LO}} = (11.5 \pm 3.5) \cdot 10^{-4} \frac{\delta m_N^{\text{str}}}{\text{MeV}}$$



$$\Rightarrow \boxed{\delta m_N^{\text{str}} = 1.5 \pm 0.8 \text{ (exp)} \pm 0.5 \text{ (th)} \text{ MeV}}$$

- uncertainty of the expected size
- nice consistency with the earlier determination of  $\delta m_N^{\text{str}}$  & lattice
- crucial ingredient:  $A_0$  from the precision PSI experiment
- can be improved systematically

# Ex. 2: Hadronic molecules



# What are HADRONIC MOLECULES ?

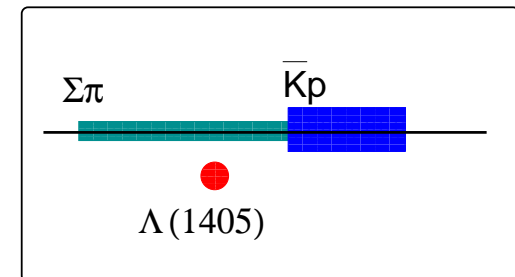
- Bound states of two hadrons in an S-wave just below a 2-particle threshold or between two close-by thresholds  $\Rightarrow$  particular decay patterns
- weak binding entails a large spatial extension
- classical examples:

★ the deuteron  $m_p + m_n = 938.27 + 939.57 \text{ MeV}$ ,  $\epsilon = 2.22 \text{ MeV}$

★ the  $\Lambda(1405)$  Dalitz et al., (1960)

$$m_\Sigma + m_\pi = 1189.37 + 139.57 = 1328.94 \text{ MeV}$$

$$m_p + m_{\bar{K}} = 938.27 + 493.68 = 1431.96 \text{ MeV}$$



★ the scalar mesons  $f_0(980), \dots$

$$m_K + m_{\bar{K}} = 2 \times 493.68 = 987.35 \text{ MeV}, m(f_0) = 976.8 \text{ MeV} \text{ [KLOE 2007]}$$

$\Rightarrow$  how to distinguish these from compact multi-quark states ?

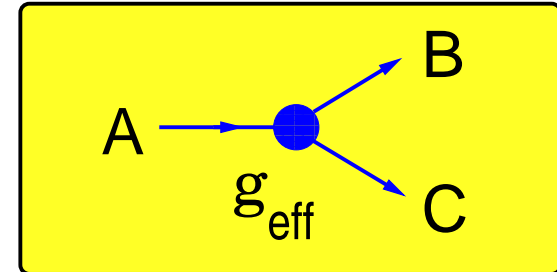
# COMPOSITENESS CRITERION

Weinberg (1963), . . . , Baru et al. (2003), . . .

- Consider S-wave decay  $A \rightarrow BC$

with a coupling constant  $g_{\text{eff}}$

and  $m_A = m_B + m_C - \varepsilon$



$$\Rightarrow \frac{g_{\text{eff}}^2}{4\pi} = 4(m_B + m_C)^{5/2} \lambda^2 \sqrt{\frac{2\varepsilon}{m_B m_C}}$$

$$\leq 4(m_B + m_C)^{5/2} \sqrt{\frac{2\varepsilon}{m_B m_C}}$$

- $\lambda^2 =$  probability to find the hadron pair in the physical state  $|A\rangle$

$\Rightarrow$

the effective coupling  $g_{\text{eff}}$  encodes the **structure information** and can be extracted **model-independently** from experiment

# PROPERTIES of the $Y(4660)$

- close to the  $f_0\psi'$  threshold:

Belle (2007)

$$m(Y(4660)) = 4664 \pm 11 \pm 5 \text{ MeV}, \quad m(f_0) + m(\psi') = 4666 \pm 10 \text{ MeV}$$

- seen only in  $e^+e^- \rightarrow \gamma_{ISR}\pi^+\pi^-\psi' \rightarrow J^{PC} = 1^{--}$
- $\pi^+\pi^-$  mass distribution strongly peaked around  $m(f_0)$
- not seen in  $e^+e^- \rightarrow \bar{D}^{(*)}D^{(*)}$  and  $e^+e^- \rightarrow J/\psi D^{(*)}\bar{D}^{(*)}$

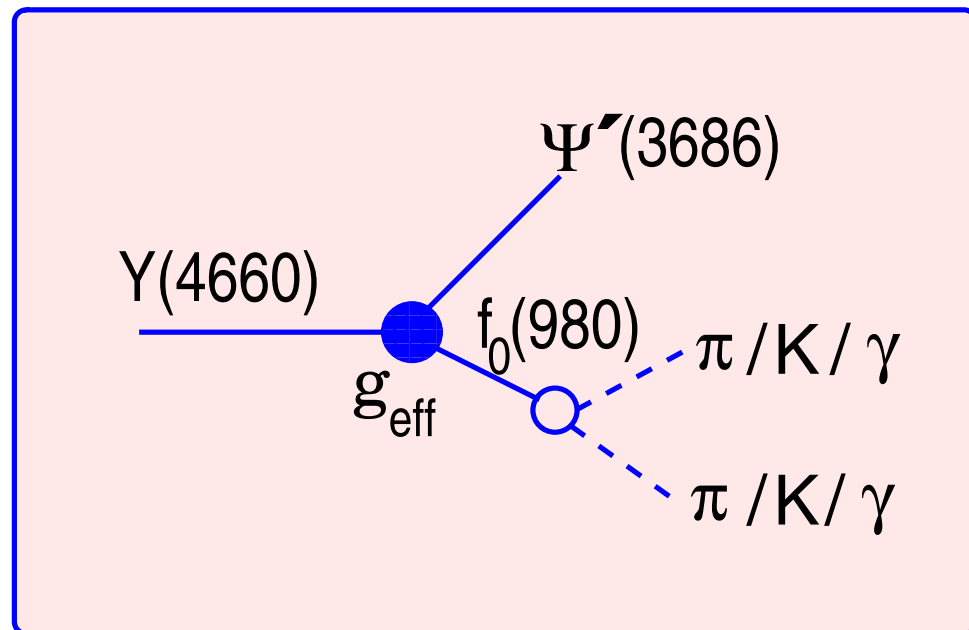
- fit to the mass distr.  $M(\psi'\pi\pi)$

with two parameters:

mass of the  $Y$

normalization

note:  $\lambda^2 = 1$



# FITS and PREDICTIONS

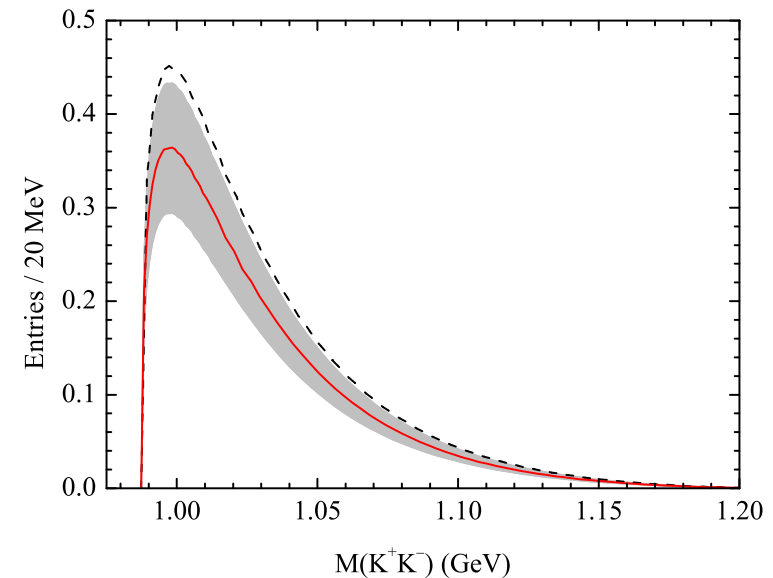
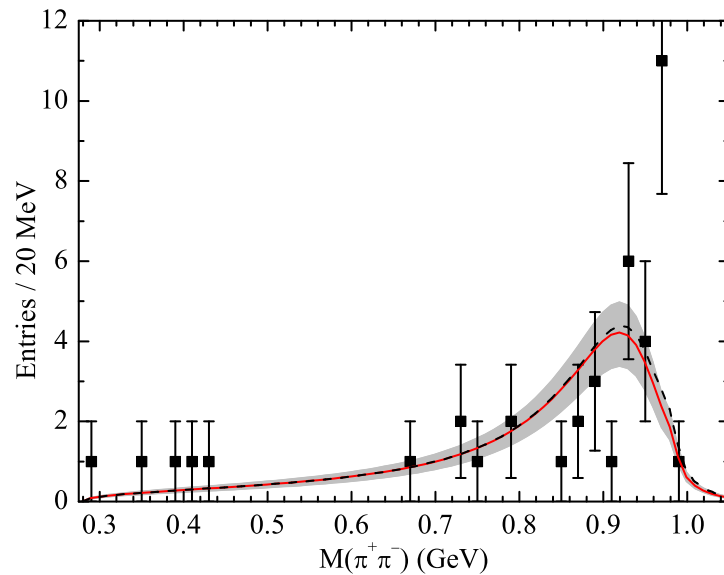
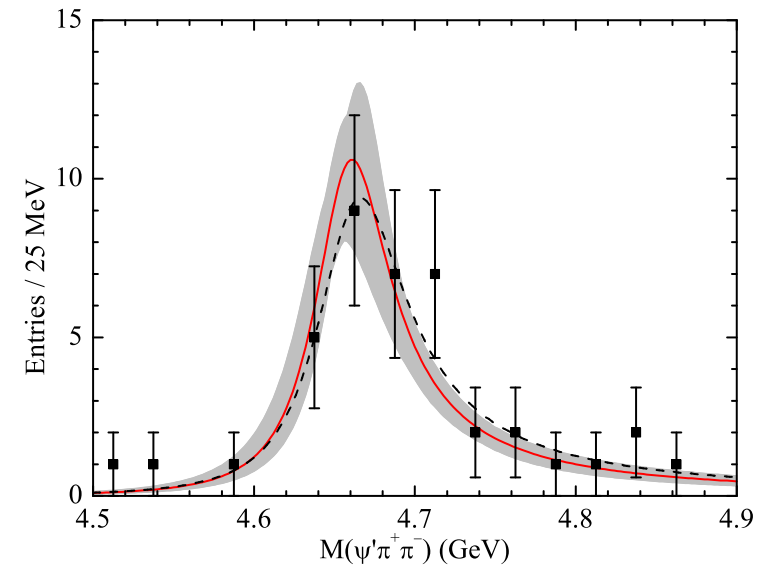
Guo, Hanhart, UGM, Phys.Lett. B **665** (2008) 26

- fit to  $M(\psi'\pi^+\pi^-)$ : [Belle (2007)]

$$m_Y = (4665_{-5}^{+3}) \text{ MeV}$$

$$\rightarrow g_{\text{eff}} = 11 \dots 14 \text{ GeV}$$

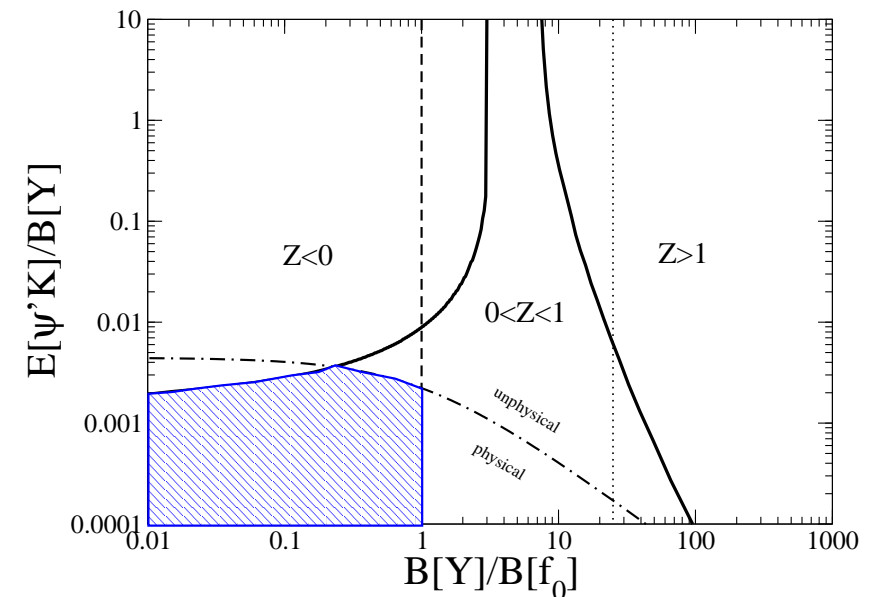
- predictions for  $\pi^+\pi^-$  and  $K^+K^-$  inv. mass distributions



# TWO- versus THREE-BODY NATURE of the $Y(4660)$

P. Hagen, H.-W. Hammer, C. Hanhart, Phys. Lett. B **696** (2011) 103

- investigate the role of the substructure of the  $f_0(980)$
- relevant scales:  $Y(4660)$  binding energy  
 $f_0(980)$  binding energy  
 $\psi' - K$  scattering length
- including compositeness criterion  
 $\Rightarrow$  determines parameter space, where  
the two-particle b.s. picture applies



# The SPIN PARTNER of the $Y(4660)$

Guo, Hanhart, UGM, Phys. Rev. Lett. **102** (2009) 242004

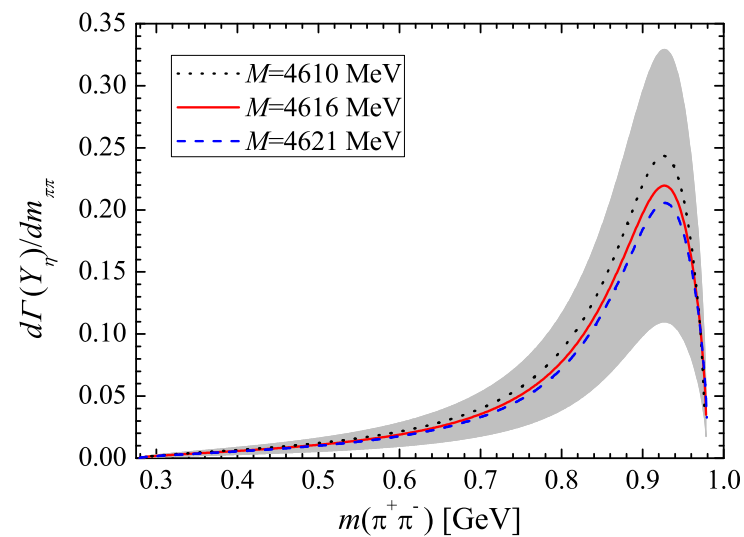
- all spin-dependent forces suppressed by powers of  $1/m_Q$ :

⇒ a spin partner of the  $Y(4660)$ , the  $Y_\eta = |f_0\eta'_c\rangle$ , with  $J^P = 0^-$ , must exist

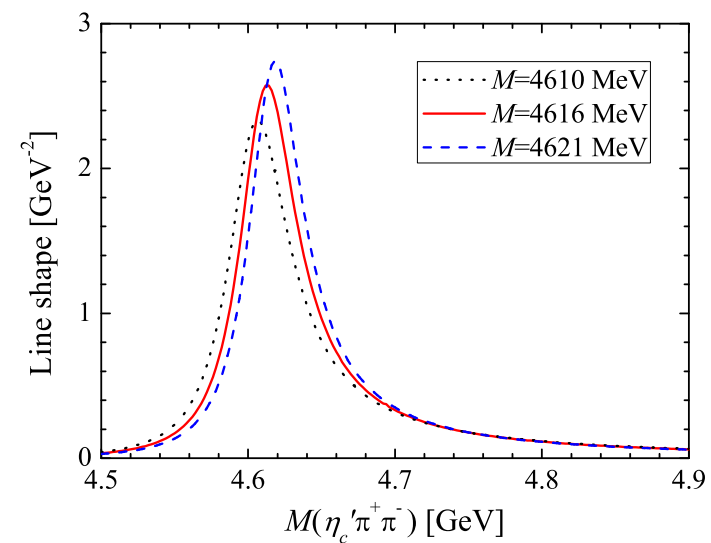
$$m(Y_\eta) = m(Y) + m(\eta'_c) - m(\psi') = 4616_{-6}^{+5} \text{ MeV}$$

- predictions

invariant mass spectrum



lineshape



# Outlook

# Making the CRC work

- Prerequisites: work towards a common aim, first step achieved
- Measures within the CRC for the next four years:
  - ★ Annual CRC workshop alternating between the sites  
[first meeting organized at KITPC Beijing, July 2-6, 2012]
  - ★ Annual CRC lecture week or summer school
  - ★ CRC focus workshops: recent developments/smaller groups
  - ★ Video-based exchanges using skype/EVO
  - ★ Joint graduate (Ph.D.) students (one chinese and one german supervisor)
  - ★ German professors will spend part of their sabbatical at IHEP/PKU
  - ★ Most projects run jointly by chinese and german PIs

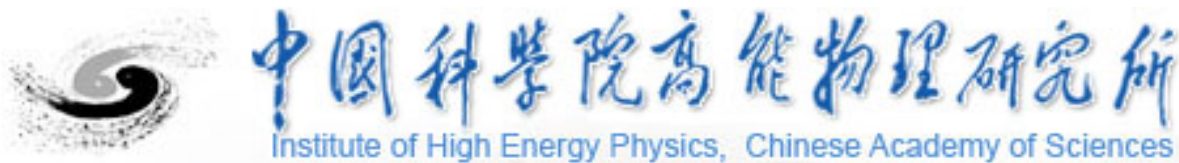
Excellent opportunities and perfect time  
for Chinese-German STRONG-QCD-CRC



- Making the first funding period a success
  - ↪ aim for over-achievement in all projects (lattice most difficult)
- Make better use of the infrastructures (HPC)
  - ↪ first step: CAS-HGF cooperation
  - ↪ next step: extend CAS-HGF cooperation to the CRC 110
- Set-up a common graduate program between CAS, PKU and german partners
  - ↪ first steps: meetings at CAS, PKU next week and in September
- Include more colleagues from PKU (and also IHEP)
  - ↪ broaden the base to include chinese nuclear physicists!
- Include more partners? [second/third funding period]
  - ↪ must be strong / 3 university limit in Germany



*Thank you for your attention !*



# SPARES

# NEW TWISTS

- BaBar observed a double-peak structure in  $\bar{B} \rightarrow \bar{K} \Lambda_c^+ \bar{\Lambda}_c^-$

→ are these the  $Y$  and the  $Y_\eta$  ?

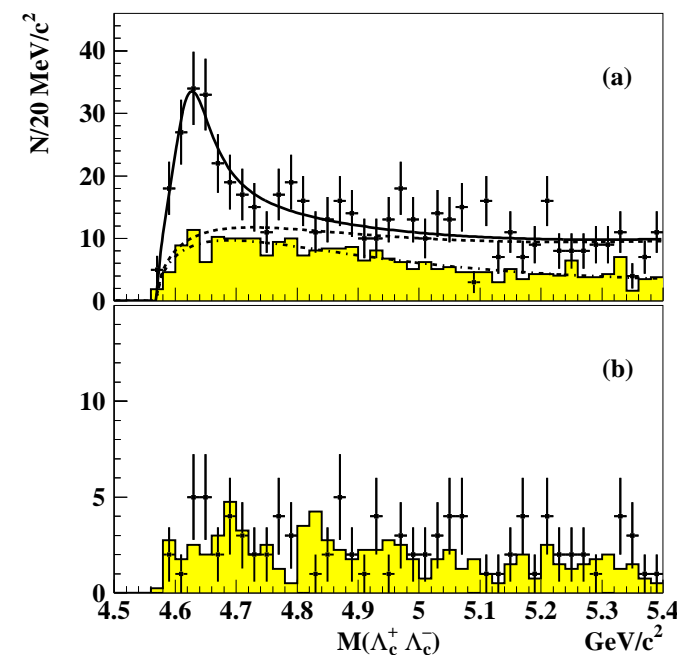
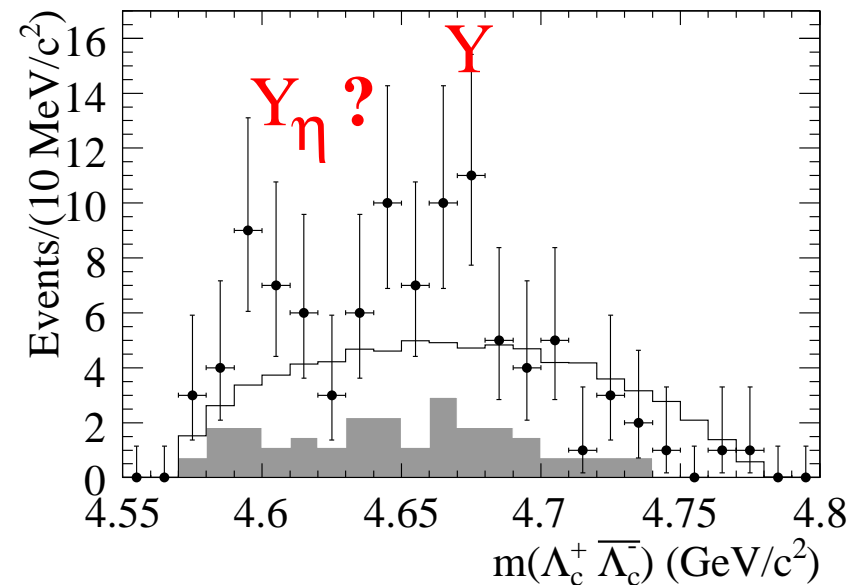
Aubert et al., PRD77 (2008)

- Belle observed a threshold enhancement in  $e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-$  with mass

$$m(X(4630)) = 4634_{-7-8}^{+8+5} \text{ MeV}$$

→ is this really a new state ?

Pakhlov et al., PRL100 (2008)



# RECONCILING the X(4630) with the Y(4660)

- include open charm channels (OCCs) in the analysis of the  $Y(4660)$ :

- assume the  $\Lambda_c^+ \Lambda_c^-$  to be the dominant OCC

- include  $\Lambda_c^+ \Lambda_c^-$  FSI from meson-exchange model

Haidenbauer, Krein (2010)

$$\Rightarrow \Gamma^{\text{tot}}(Y) = \frac{3}{2} \Gamma(Y \rightarrow \psi' \pi \pi) + \Gamma(Y \rightarrow \Lambda_c^+ \Lambda_c^-)$$

$$\Gamma(Y \rightarrow \Lambda_c^+ \Lambda_c^-) = \frac{g_{Y \Lambda_c \Lambda_c}^2}{|J(M)|^2} \frac{p}{6\pi} \left( 1 + \frac{2M_{\Lambda_c}^2}{M^2} \right) \theta(M - 2M_{\Lambda_c})$$

- fit to Belle mass distributions with 3 parameters:

normalization  $\mathcal{N}$

mass of the  $Y$ ,  $m(Y)$

coupling constant  $g_{Y \Lambda_c \Lambda_c}$

# RECONCILING the X(4630) with the Y(4660) cont'd

- consistent w/ Belle data

$$m(Y) = 4662^{+0.1}_{-0.2} \text{ MeV},$$

$$g_{Y\Lambda_c\Lambda_c} = 0.7 \pm 0.1$$

$$\frac{\Gamma(Y \rightarrow \Lambda_c^+ \Lambda_c^-)}{\Gamma(Y \rightarrow \psi' \pi^+ \pi^-)} = 11.5$$

- prediction for the spin partner:

$$\frac{\Gamma(Y_\eta \rightarrow \Lambda_c^+ \Lambda_c^-)}{\Gamma(Y_\eta \rightarrow \psi' \pi^+ \pi^-)} = 2.7$$

⇒ testable prediction

e.g. in  $B^\pm \rightarrow K^\pm \eta'_c \pi^+ \pi^-$

and  $B^\pm \rightarrow K^\pm \Lambda_c^+ \Lambda_c^-$

